

(Blitzer, chapters 5 and 6)

1. Verify the following trigonometric identities:

a.  $\frac{\tan \theta + \cot \theta}{\sec \theta} = \csc \theta$  (10)

b.  $\cos^4 \theta - \sin^4 \theta = 1 - 2\sin^2 \theta$  (10)

c.  $\frac{\sin(\alpha + \beta)}{\cos \alpha \cos \beta} = \tan \alpha + \tan \beta$  (10)

2. Find the exact value of  $\cos(45^\circ - 30^\circ)$ . (10)

3. Solve: (10)

$$2 \sin^2 x - 3 \sin x - 2 = 0, \quad 0 \leq x < 2\pi$$

4. Solve each triangle (express angles to nearest degree and length to nearest tenth).

a.  $a = 5, b = 7, C = 42^\circ$  (10)

b.  $A = 44^\circ, B = 25^\circ, a = 12$  (10)

5. Convert the equation to polar coordinates: (5)

$$3x + y = 7$$

6. Convert the equation to Cartesian coordinates: (5)

$$r = 6 \cos \theta + 4 \sin \theta$$

7. Find all fifth roots of 32. Express the values rounded to the nearest tenth. (20)

8. Sketch the graph for:

$$r = 1 - \sin \theta. \quad (10)$$